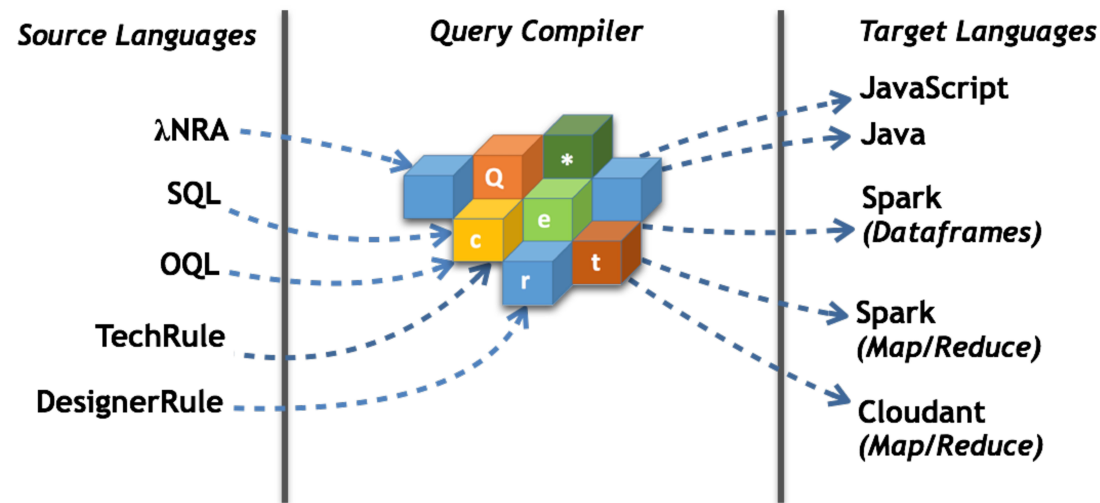

Handling Environments in a Nested Relational Algebra with Combinators and an Implementation in a Verified Query Compiler

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1. Verified Query Compiler



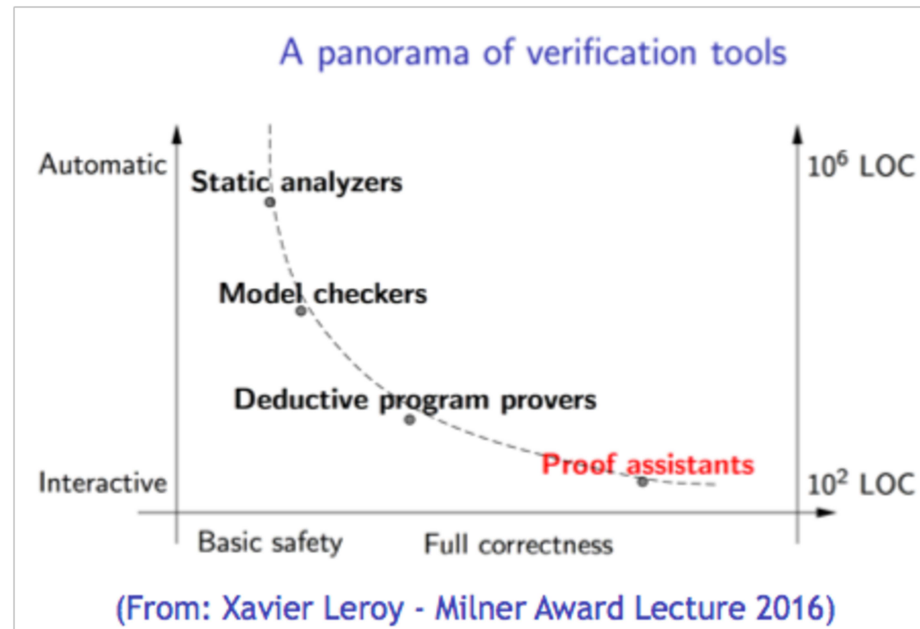
Why?

- ▶ Bugs are costly, security & privacy, guarantee access control, ...
- ▶ Define and check new optimizations
- ▶ Specify and compile new languages (e.g., DSLs)

How?

- ▶ Implemented with the Coq Proof Assistant
- ▶ Proof that the compiler preserves semantic is machine-checked

1. Verified Query Compiler



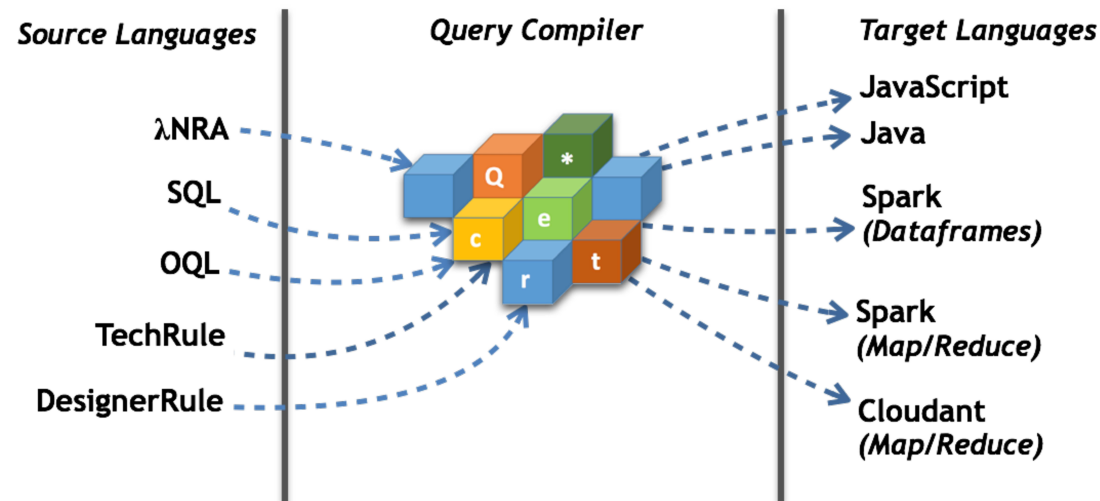
Some recent successes:

- ▶ CompCert (C compiler) ; Yxv6 (file system)
- ▶ seL4 (secure microkernel) ; HACMS program (secure drones)

Database-related: (Also: Cosette at SIGMOD'2017)

- ▶ DataCert [ESOP'2014]; mini-XQuery [CPP'2011]; RDBMS [POPL'2010]
- ▶ Optimizer Generator in Coko-Kola Project [SIGMOD 1996,1998...]

1. Verified Query Compiler



SQL:

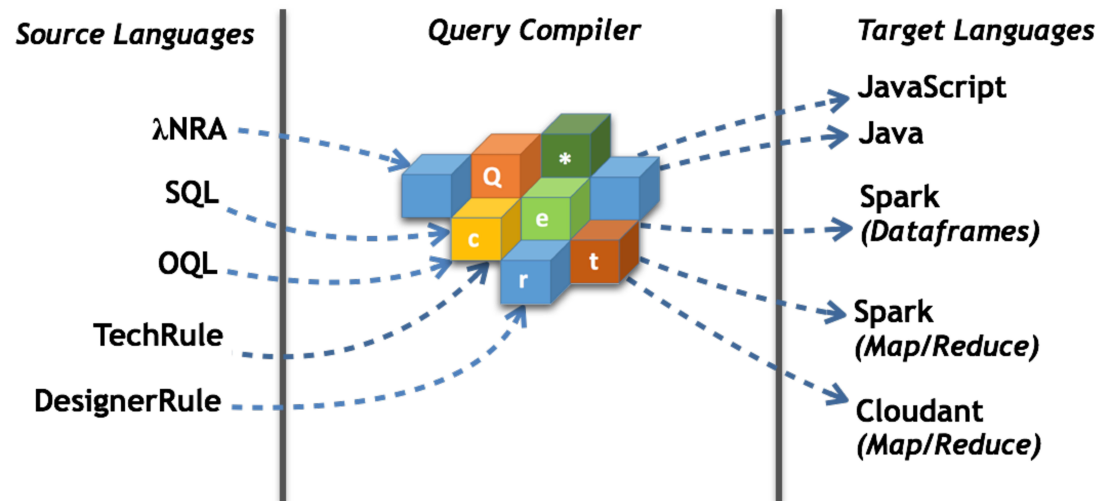
```
SELECT *
FROM (SELECT name,age FROM employees
      UNION ALL
      SELECT name,age FROM students) AS persons
WHERE age = 32;
```

OQL (yes ODMG one):

```
define view as
  select struct(name:c->name, purchased: p->name)
  from c in Clients, p in Purchases
  where p->cid = c->id;

select x.name from x in view where x.purchased = "Tomatoe"
```


1. Verified Query Compiler



λ NRA:

```
Customers.filter{ p => p.age = 32 }.map{ p => p.salary }.avg()
```

IBM's ODM Insights Designer Rules:

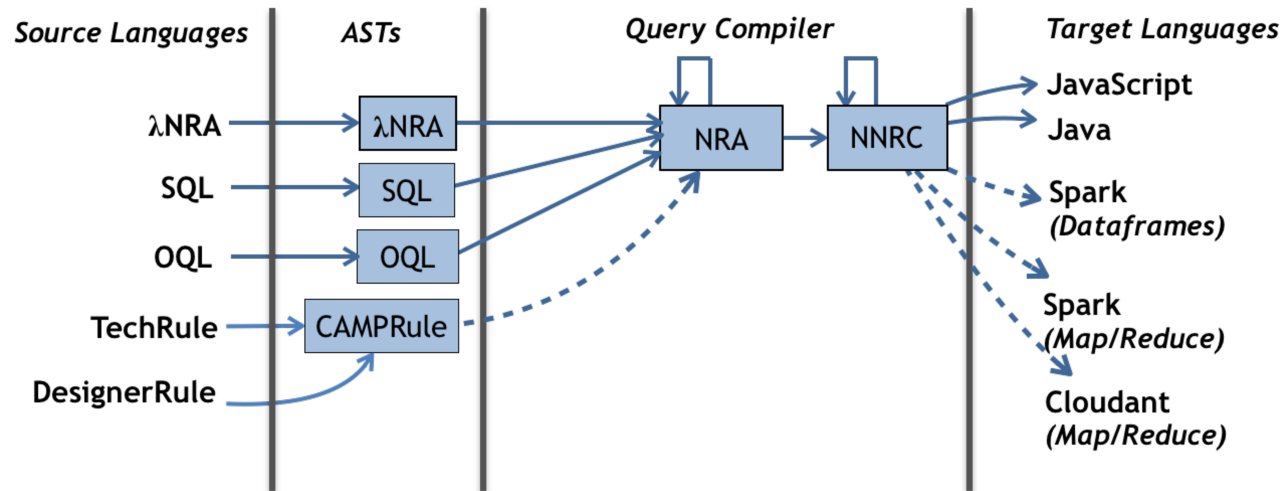
```
define 'test05' as detailed below, evaluated every minute.
```

```
definitions
```

```
set 'test05' to the number of Customers,  
    where the age of each Customer equals 32;
```

```
use 'test05' as the result.
```

1. Verified Query Compiler



- ▶ Like any other query compiler:
 - ▷ Source to AST to Logical Algebra to Physical Plan to Code
 - ▷ Emitted code executed by runtime (e.g., JVM, Database)
- ▶ But:
 - ▷ Each intermediate language needs a complete formal semantics
 - ▷ Logical: Nested Relational Algebra (from Cluet & Moerkotte)
 - ▷ "Physical": Named Nested Relational Calculus (from Van den Bussche & Vansummeren).

1. Verified Query Compiler

Lemma `tselect_union_distr q0 q1 q2 : (* Equivalence *)`

$\sigma\langle q_0 \rangle(q_1 \cup q_2) \Rightarrow \sigma\langle q_0 \rangle(q_1) \cup \sigma\langle q_0 \rangle(q_2).$

Proof. ... `Qed.`

Definition `select_union_distr_fun q := (* Functional rewrite *)`

`match q with`

`| NRAEnvSelect q0 (NRAEnvBinop AUnion q1 q2) =>`

`NRAEnvBinop AUnion (NRAEnvSelect q0 q1) (NRAEnvSelect q0 q2)`

`| _ => q`

`end.`

Proposition `select_union_distr_fun_correctness q: (* Rewrite is correct *)`

`select_union_distr_fun q \Rightarrow q.`

Proof.

`tprove_correctness q.`

`apply tselect_union_distr.`

Qed.

Challenges:

- ▶ Depth of specification (equality, what's an equivalence, typing...).
- ▶ **Handling environments** in intermediate representations

2. Handling Environments

With variables (i.e., lambdas):

$$\mathbf{map}(\lambda a.(a.city))(\mathbf{map}(\lambda p.(p.addr))(P)) \equiv \mathbf{map}(\lambda p.((p.addr).city))(P)$$

$$\mathbf{map}(\lambda x.(e))(\mathbf{map}(\lambda y.(u))(v)) \equiv \mathbf{map}(\lambda y.(\underline{e[u/x]}))(v)$$

Without variables (i.e., combinators):

$$\chi_{\langle \mathbf{ln}.a.city \rangle}(\chi_{\langle [a:\mathbf{ln}] \rangle}(\chi_{\langle \mathbf{ln}.p.addr \rangle}(\chi_{\langle [p:\mathbf{ln}] \rangle}(q)))) \equiv \chi_{\langle \mathbf{ln}.p.addr.city \rangle}(\chi_{\langle [p:\mathbf{ln}] \rangle}(q))$$

$$\chi_{\langle q_1 \rangle}(\chi_{\langle q_2 \rangle}(q)) \equiv \chi_{\langle \underline{q_1 \circ q_2} \rangle}(q)$$

- ▶ Rewrites with variables/binders is harder (e.g., here involves substitution)
- ▶ Rewrites with combinators is easier (e.g., here plan composition)
- ▶ Correctness of binders manipulation notoriously difficult to mechanize
- ▶ See: POPLMark, and once again, Cherniack and Zdonik, SIGMOD 1996!

2. Handling Environments

With variables (i.e., lambdas):

$\mathbf{map}(\lambda \underline{p}.([\underline{p} : \underline{p}, k : \mathbf{filter}(\lambda \underline{c}.(\underline{p}.age < \underline{c}.age))(\underline{p}.child))](P)$

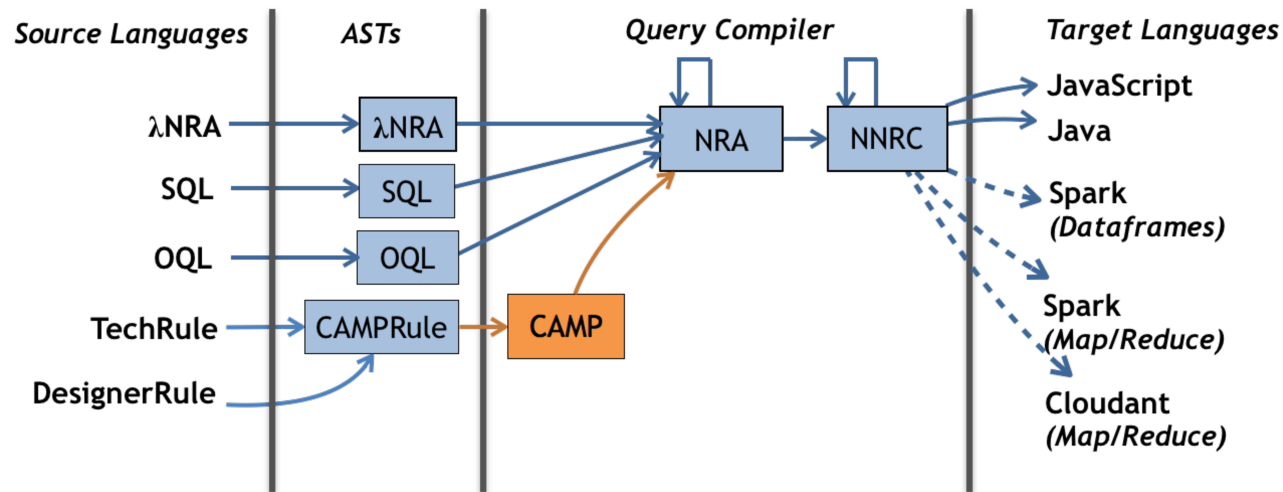
Without variables (i.e., combinators):

$\chi \left\langle \left[p : \underline{\mathbf{In}.p}, k : \chi_{\langle \underline{\mathbf{In}.c} \rangle} \left(\sigma_{\langle \underline{\mathbf{In}.p}.age < \underline{\mathbf{In}.c}.age \rangle} \left(\bowtie^d \left\langle \chi_{\langle \underline{[c:\mathbf{In}]} \rangle}(\underline{\mathbf{In}.p}.child) \right\rangle (\{\mathbf{In}\}) \right) \right] \right\rangle \left(\chi_{\langle \underline{[p:\mathbf{In}]} \rangle} (P) \right)$

Cost of reification:

- ▶ 5 iterators instead of 2
- ▶ nesting depth 3 instead of 2
- ▶ Use of dependent join (\bowtie^d) to combine p and c bindings

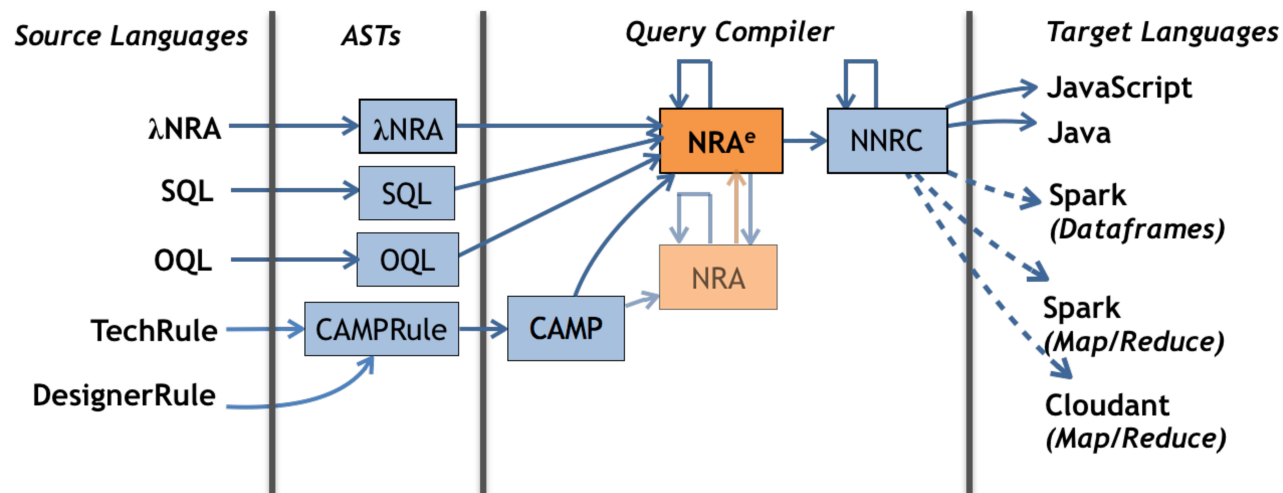
2. Handling Environments



Sensitive to source language semantics & Encoding
e.g., for Designer Rules DSL:

- ▶ Environment = Source language variables + current item being matched
- ▶ Initial plans: from 400 to 2500 operators, depth 7 to 13
- ▶ Reification of environment manipulation impedes optimization

3. Nested Relational Algebra with Combinators

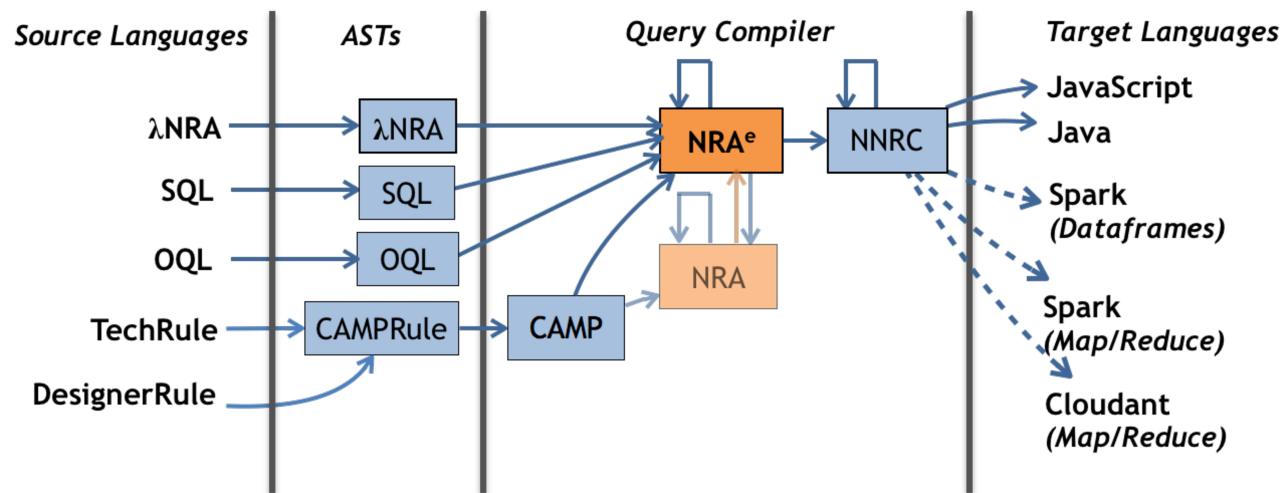


NRA Syntax $q ::= d \mid \underline{\mathbf{In}} \mid \underline{q_2 \circ q_1} \mid \boxplus q \mid q_1 \boxtimes q_2 \mid \chi_{\langle q_2 \rangle}(q_1) \mid \sigma_{\langle q_2 \rangle}(q_1) \mid q_1 \times q_2 \mid \bowtie^d_{\langle q_2 \rangle}(q_1) \mid q_1 \parallel q_2$

NRA Semantics $\vdash q @ d \Downarrow_a d'$

- ▶ $\vdash \mathbf{In} @ \boxed{d} \Downarrow_a d$ (current value)
- ▶ $q_1 \circ q_2$ (sets current value in q_1 to q_2)
- ▶ $\boxplus q$: flatten, $q.a$, π , ...; $q_1 \boxtimes q_2$: $q_1 = q_2$, $q_1 \cup q_2$, \oplus (record concatenation), ...
- ▶ χ (map) ; σ (selection) ; \times (Cartesian product) ; \bowtie^d (dependent join)

3. Nested Relational Algebra with Combinators



$$\begin{aligned}
 \text{NRA}^e \text{ Syntax } q ::= & d \mid \mathbf{In} \mid q_2 \circ q_1 \mid \boxplus q \mid q_1 \boxtimes q_2 \mid \chi_{\langle q_2 \rangle}(q_1) \\
 & \mid \sigma_{\langle q_2 \rangle}(q_1) \mid q_1 \times q_2 \mid \bowtie^d_{\langle q_2 \rangle}(q_1) \mid q_1 \parallel q_2 \\
 & \mid \underline{\mathbf{Env}} \mid \underline{q_2 \circ^e q_1} \mid \underline{\chi_{\langle q \rangle}^e}
 \end{aligned}$$

$$\text{NRA}^e \text{ Semantics } \underline{\gamma} \vdash q @ d \Downarrow_a d'$$

- ▶ $\boxed{\gamma} \vdash \mathbf{Env} @ d \Downarrow_a \gamma$ (current environment)
- ▶ $q_1 \circ^e q_2$ (sets current environment in q_1 to q_2)
- ▶ $q_1 \circ^e \mathbf{Env} \oplus [x : q_2]$ (adding x to environment)

3. Nested Relational Algebra with Combinators

With variables (i.e., lambdas):

$$\mathbf{map}(\lambda \underline{p}.([\underline{p} : \underline{p}, k : \mathbf{filter}(\lambda \underline{c}.(\underline{p}.age < \underline{c}.age))(\underline{p}.child))])(P)$$

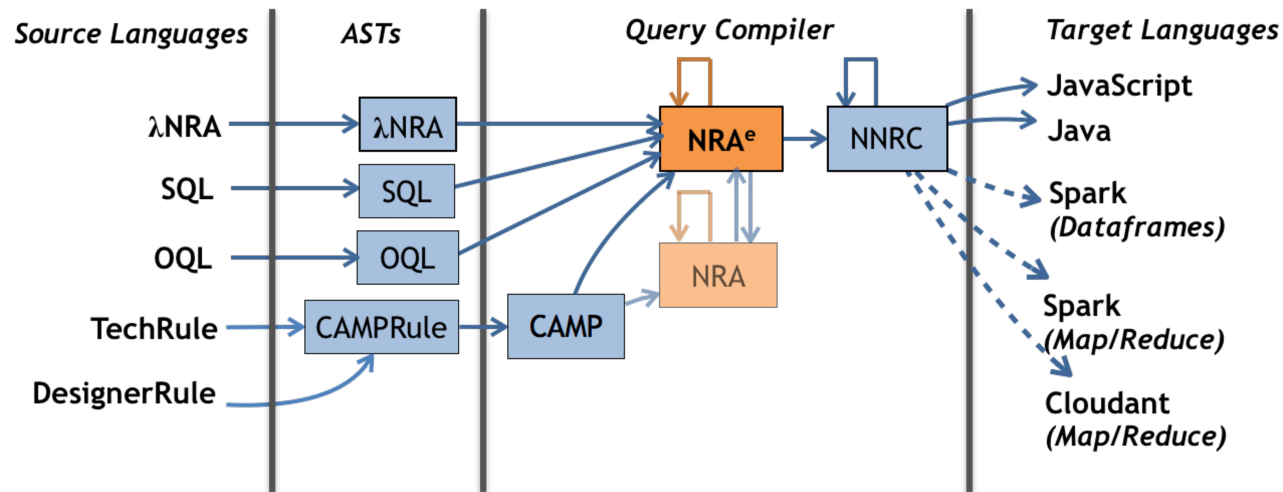
With NRA^e:

$$\chi \left\langle [p : \underline{\mathbf{Env}.p}, k : \sigma_{(\underline{\mathbf{Env}.p}.age < \underline{\mathbf{Env}.c}.age) \circ^e (\underline{\mathbf{Env} \oplus [c:\mathbf{In}]})}(\underline{\mathbf{Env}.p}.child)] \circ^e \underline{[p : \mathbf{In}]} \right\rangle (P)$$

Cost of reification:

- ▶ Same number of iterators: 2
- ▶ Same nesting depth: 3
- ▶ No added (dependent) join

3. Nested Relational Algebra with Combinators



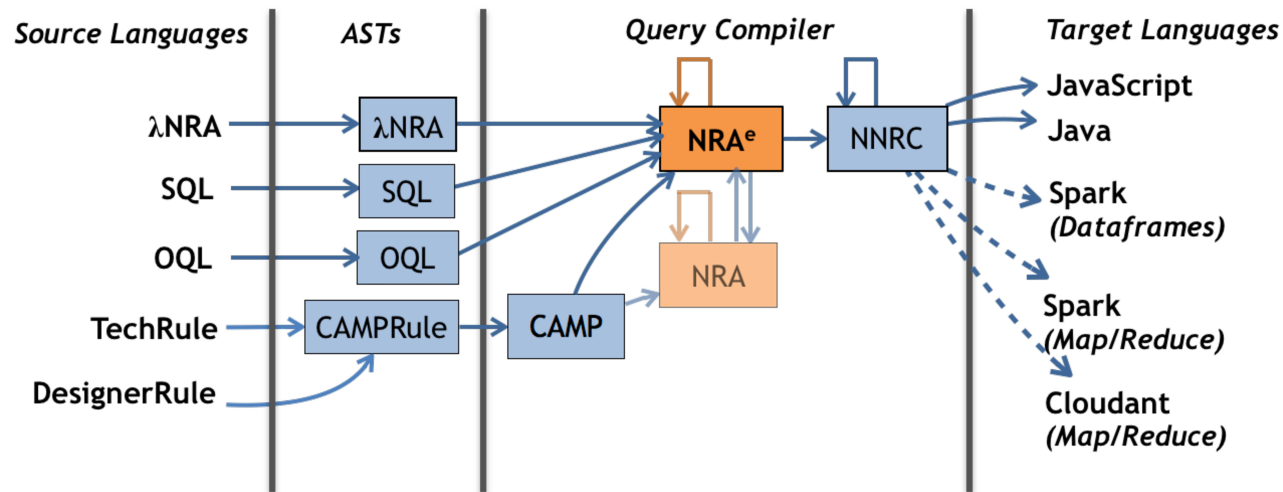
Lifting theorem

- All existing equivalences for NRA carry over to NRA^e

$$\sigma_{\langle q_0 \rangle}(q_1 \cup q_2) \equiv \sigma_{\langle q_0 \rangle}(q_1) \cup \sigma_{\langle q_0 \rangle}(q_2)$$

$$\chi_{\langle q_1 \rangle}(\chi_{\langle q_2 \rangle}(q)) \equiv \chi_{\langle q_1 \circ q_2 \rangle}(q)$$

3. Nested Relational Algebra with Combinators



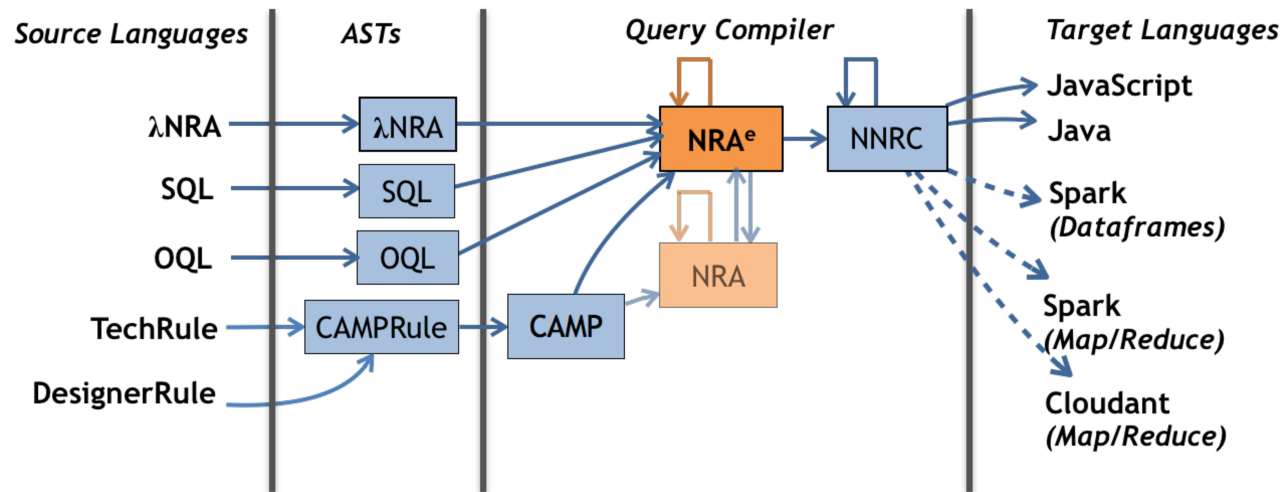
Lifting theorem

- All existing equivalences for NRA carry over to NRA^e
- True even if sub-plans parameters contain NRA^e operators!

$$\forall q_1, q_2, q \in \text{NRA}, \chi_{\langle q_1 \rangle}(\chi_{\langle q_2 \rangle}(q)) \equiv_a \chi_{\langle q_1 \circ q_2 \rangle}(q)$$

$$\implies \forall q_1, q_2, q \in \text{NRA}^e, \chi_{\langle q_1 \rangle}(\chi_{\langle q_2 \rangle}(q)) \equiv_e \chi_{\langle q_1 \circ q_2 \rangle}(q)$$

3. Nested Relational Algebra with Combinators



Lifting theorem

- Yes, the proof of that theorem has been mechanized

```
Fixpoint lift_nra_context (c:nra_ctxt) : nraenv_core_ctxt := ...
```

```
Theorem contextual_equivalence_lifting (c1 c2:nra_ctxt) :
```

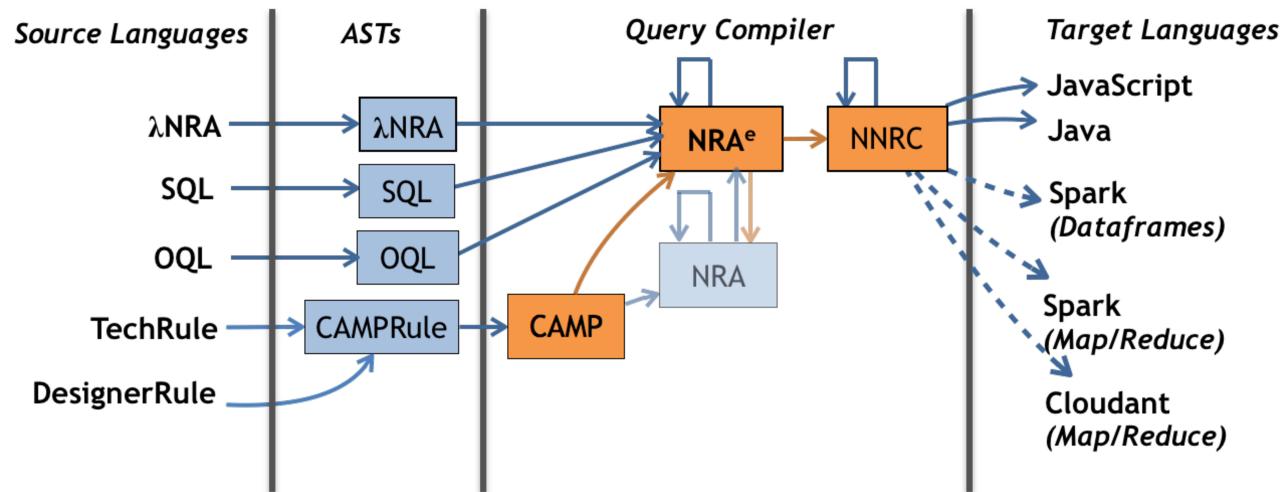
```
c1  $\equiv_a$  c2 -> lift_nra_context c1  $\equiv_e$  lift_nra_context c2.
```

Proof.

```
apply lift_nra_context_proper.
```

Qed.

3. Nested Relational Algebra with Combinators



Translations In-Out of NRA^e

- ▶ from NRA^e to NNRC and NRA
- ▶ from CAMP and NRA^λ (without blowup) to NRA^e

3. Nested Relational Algebra with Combinators

- from NRA^e to NRA in \LaTeX

$$\begin{aligned}
 \llbracket d \rrbracket_a &= d \\
 \llbracket \text{In} \rrbracket_a &= \text{In}.D \\
 \llbracket q_2 \circ q_1 \rrbracket_a &= \llbracket q_2 \rrbracket_a \circ ([E : \text{In}.E] \oplus [D : \llbracket q_1 \rrbracket_a]) \\
 \llbracket \boxplus q \rrbracket_a &= \boxplus \llbracket q \rrbracket_a \\
 &\dots
 \end{aligned}$$

Figure 4: From NRA^e to NRA \clubsuit .

$$\boxed{\llbracket q \rrbracket_a = q'}$$

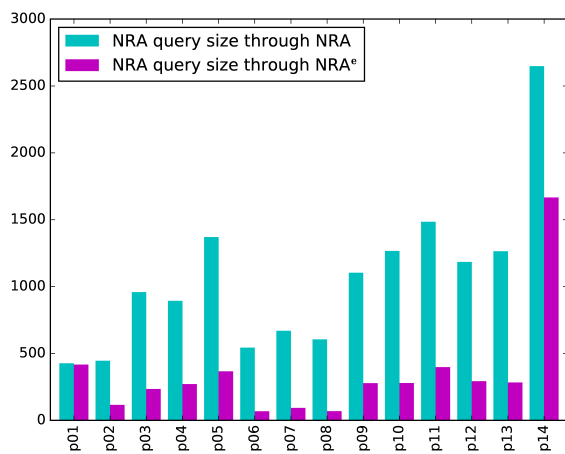
- from NRA^e to NRA in Coq (+ correctness proofs)

```

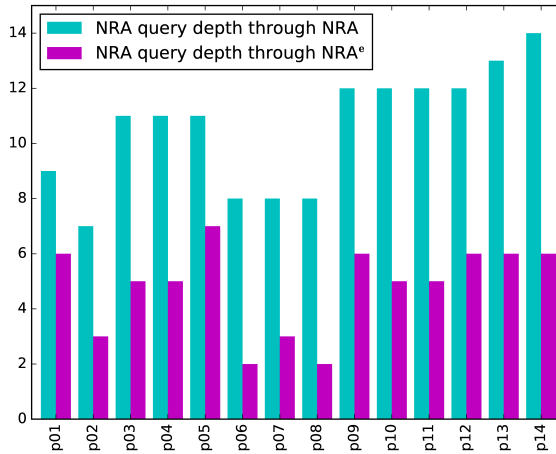
Fixpoint nra_of_nraenv_core (ae:nraenv_core) : nra :=
  match ae with
  | ANID => nra_data
  | ANConst d => (AConst d)
  | ANApp ea1 ea2 => AApp (nra_of_nraenv_core ea1)
                        (nra_wrap (nra_of_nraenv_core ea2))
  | ANUnop u ae1 => AUnop u (nra_of_nraenv_core ae1)
  ...

```

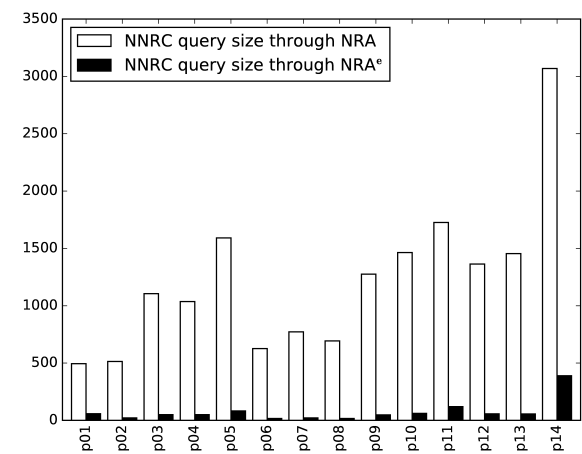
3. Nested Relational Algebra with Combinators



(a) Initial plan sizes.



(b) Initial plan depths.

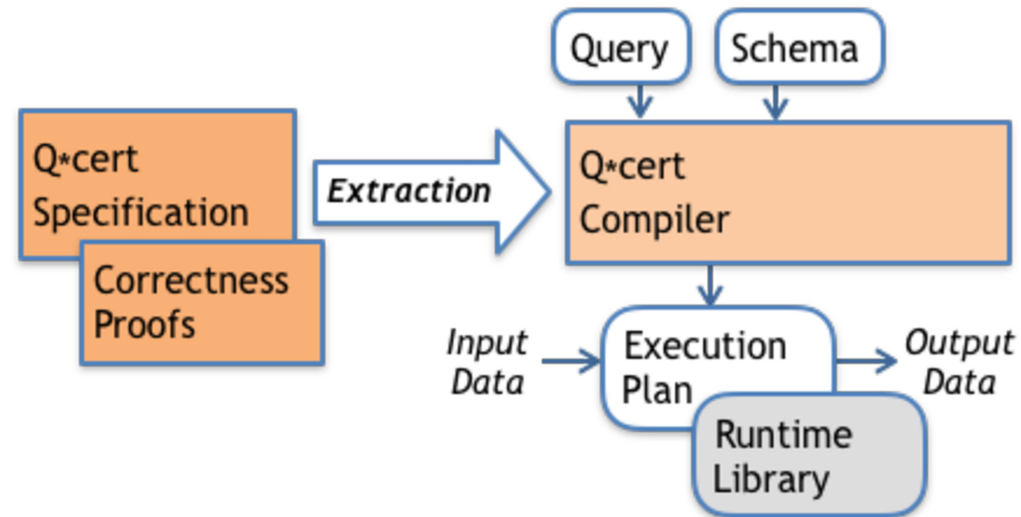


(c) Emitted NNRC sizes.

Other Practical Benefits:

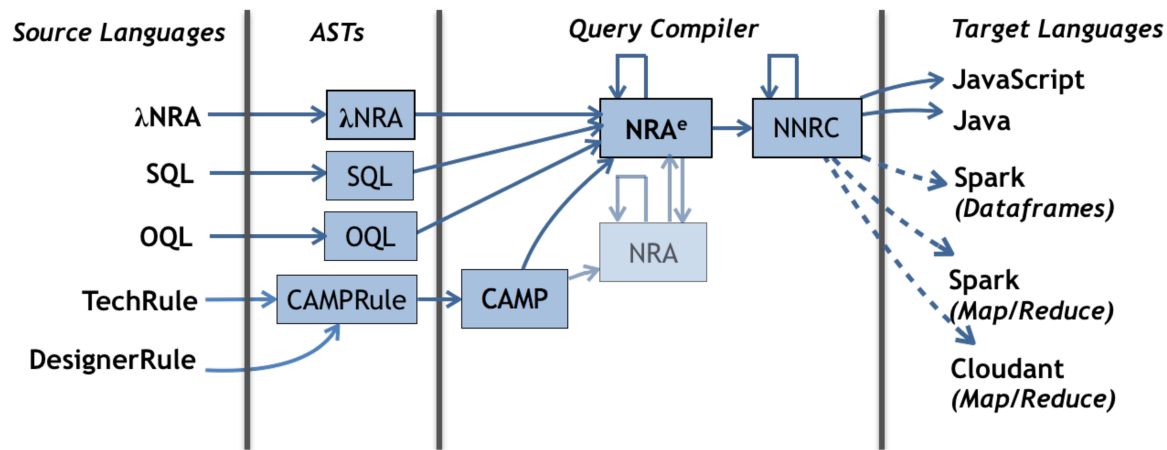
- ▶ NRA^e gives an elegant way to represent 'let' bindings:
 - ▷ e.g., view definitions for SQL and OQL ($q \circ^e \mathbf{Env} \oplus [\text{view} : q_v]$)
 - ▷ e.g., common subexpression elimination in query plans
- ▶ Optimization for ODM Designer Rules
 - ▷ Combination of existing and new NRA rewrites (~100)
 - ▷ Benchmarks: plan size and depth; Optimizer effectiveness

4. Implementation



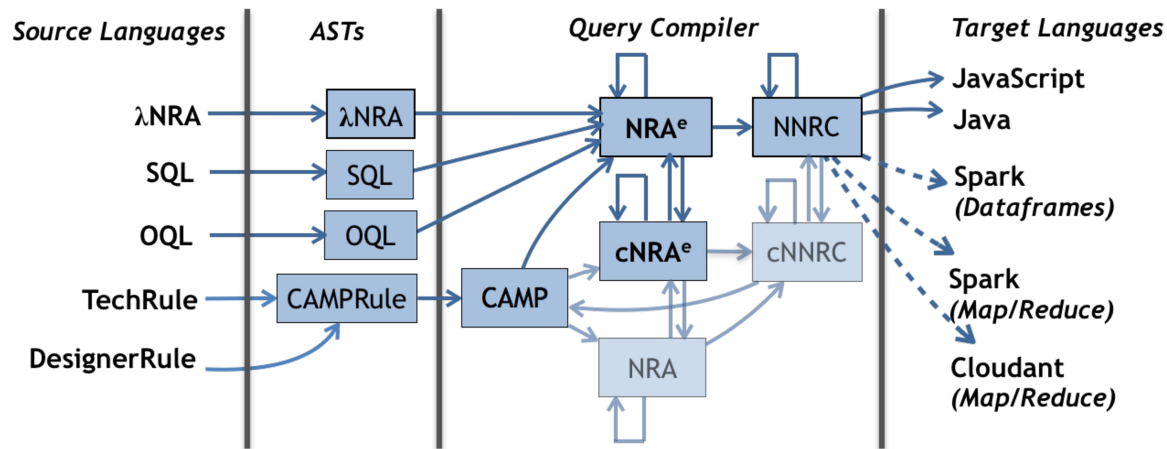
- ▶ Around: 40k lines of code ; 45k lines of proofs
- ▶ $\text{Coq} \mapsto \text{OCaml (90k)} \mapsto \text{native code or JavaScript}$
- ▶ Optimizer: naive cost model, directed rewrites, until fixpoint
 - ▷ Designed for extensibility (add/remove optimizations; change cost)
 - ▷ Timed up to a few seconds for large plans (e.g., TPC-H queries)
- ▶ Small runtimes for now (Java, Javascript and Scala)

4. Implementation



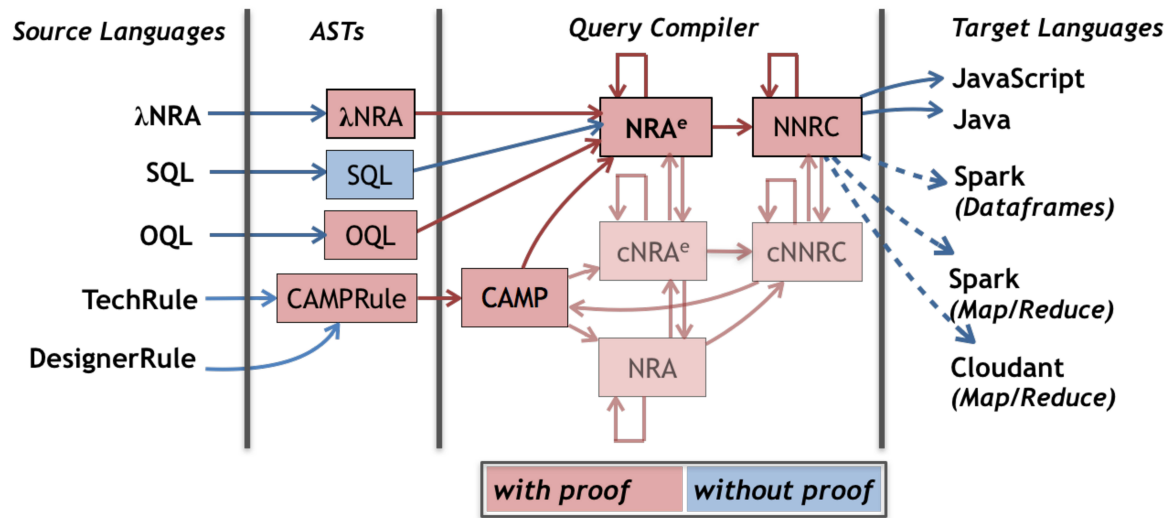
- Type System (Wadlerfest'2016):
 - ▷ Support for objects (used in OQL and Designer rules)
 - ▷ Support for optional types (e.g., for null values)

4. Implementation



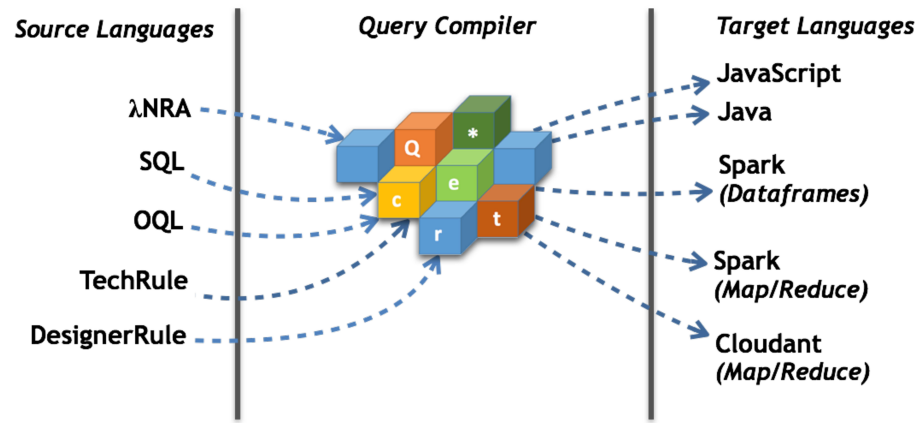
- ▶ Type System (Wadlerfest'2016):
 - ▷ Support for objects (used in OQL and Designer rules)
 - ▷ Support for optional types (e.g., for null values)
- ▶ Full NRA^e with OrderBy, GroupBy and Joins

4. Implementation



- ▶ Type System (Wadlerfest'2016):
 - ▷ Support for objects (used in OQL and Designer rules)
 - ▷ Support for optional types (e.g., for null values)
- ▶ Full NRA^e with GroupBy and Joins
- ▶ Proof coverage matters & garbage-in garbage-out

Conclusion



<http://querycert.github.io/>

- ▶ Query compiler in Coq; Large subset of compiler proved correct
- ▶ NRA^e : Easier rewrites & proofs ; Keep plan simple
- ▶ Some future directions: (suggestions or applications welcome!)
 - ▷ End to end certification (e.g., SQL to JavaScript)
 - ▷ Certified runtimes (including e.g., Join algorithms)
 - ▷ Other languages (e.g., SQL++) or backend
 - ▷ Grow the query optimizer (Join reordering, Cost model...)